

Theoretical study on the micro-scale oxidation of resin-infused carbon ablators

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Abstract

When subjected to high enthalpy air, phenolic-impregnated carbon-based ablative thermal protection systems undergo oxidation of their carbon fiber substrate and carbonized phenolic matrix. The oxidation process is governed by the competition between reaction and diffusion within the porous material and occurs at a range of depths depending on the flow conditions, the material chemical composition, and the material micro-structure. This study aims to examine the effects of the distribution of carbonized phenolic matrix on the oxidation behavior of carbon fiber materials, with the goal of guiding future material design. The oxidation is simulated on ideal geometries and on representations of actual fibrous carbon preforms obtained from X-ray microtomography. Diffusion is simulated using a random walk technique with a linear interpolation method for surface collisions. Oxidation reactions are simulated using a sticking probability law. It is shown that the oxidation characteristics, particularly the oxidation depth, are strong functions of the Thiele number and that the effect of the matrix distribution within the fibers is more pronounced at low Thiele regimes.

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Nomenclature

Greek

ϵ	Porosity, -
Ω	Molar volume, $\text{m}^3 \cdot \text{mol}^{-1}$
Φ	Thiele number, -
ρ	Density, kg m^{-3}
θ	Average cylinder angle, rad

Symbols

A	Reactivity contrast, -
\vec{e}	Unit vector, -
C	Concentration, $\text{mol} \cdot \text{m}^{-3}$
D	Diffusion coefficient, $\text{m}^{-2} \cdot \text{s}^{-1}$
d	diameter, m
J	Molar oxidation flux, $\text{mol} \cdot \text{m}^{-2} \cdot \text{s}^{-1}$

k	Reactivity, $\text{m} \cdot \text{s}^{-1}$
n	Surface normal, -
r	Radius, m
S	Surface function
s	Specific surface area, m^{-1}
t	Time, s
v	Recession velocity, $\text{m} \cdot \text{s}^{-1}$
x	Mass fraction, -
z	Matrix recession depth, m

Subscripts

eff	effective
f	fiber
m	matrix
p	pore

1. Introduction

Atmospheric entry missions require the use of thermal protection systems (TPS) to mitigate the aerothermal loads experienced at hypersonic conditions. One successful class of TPS materials are light-weight carbon phenolic ablaters, built upon a carbon fiber preform and impregnated with phenolic resin. The phenolic impregnation improves mechanical properties [1] and limits oxygen penetration into the material. During entry, the phenolic resin pyrolyzes [2], causing a blow back of pyrolysis gases into the boundary layer. During pyrolysis, the phenolic resin undergoes carbonization, also referred to as charring, which produces a structure of pseudo-graphitic carbon left within the carbon

11 fiber substrate. Depending on the impregnation and curing process of the phe-
12 nolic resin, as well as the pyrolysis conditions, the carbonized resin can have a
13 variety of distributions, densities, and mass fractions [3]. After full pyrolysis,
14 the remaining carbonaceous material, composed of carbon fiber substrate and
15 carbonized phenolic matrix, undergoes mass loss due to oxidation, sublimation,
16 and spallation[4] (mass loss due to mechanical forces of friction and shear).

17 Many current ablation material response models, based on the work of
18 Kendall et. al [5], rely on a surface ablation hypothesis. Heritage models do not
19 account for the micro-structure of the material and the in-depth oxidation that
20 can occur due to the diffusion of reactants into the material. Because of the high
21 porosity and range of oxidation depths, the micro-scale oxidation behavior must
22 be understood and incorporated into the next generation of volume averaged
23 models [6] in order to guide material design.

24 A micro-scale oxidation model was first proposed by Lachaud and Vignoles
25 [7] and applied to ideal representations of carbon fiber substrates [8]. Our
26 research group then studied the inclusion of a phenolic phase on ideal represen-
27 tations of carbon fiber substrates in order to develop a preliminary understand-
28 ing of the effects of resin distribution on the oxidation process [9]. However,
29 such ideal geometries do not adequately capture the complex fiber clusters and
30 structures evidenced in real carbon fiber substrates under a scanning electron
31 microscope [10]. An effort was made to obtain a realistic representation of car-
32 bon fiber substrates through the use of hard X-ray micro-tomography [10, 11].
33 The resulting tomography images, with sub-micron voxel sizes, provide a digital
34 representation of the real material that can be used to calculate material prop-
35 erties or simulate material response [12, 13]. A computational framework, called
36 Porous Materials Analysis (PuMA) [14] was developed at the NASA Ames Re-
37 search Center to handle these large micro-tomography datasets. PuMA includes
38 an implementation of the oxidation method proposed by Lachaud and Vignoles
39 [7], modified to oxidize large datasets using parallel computing.

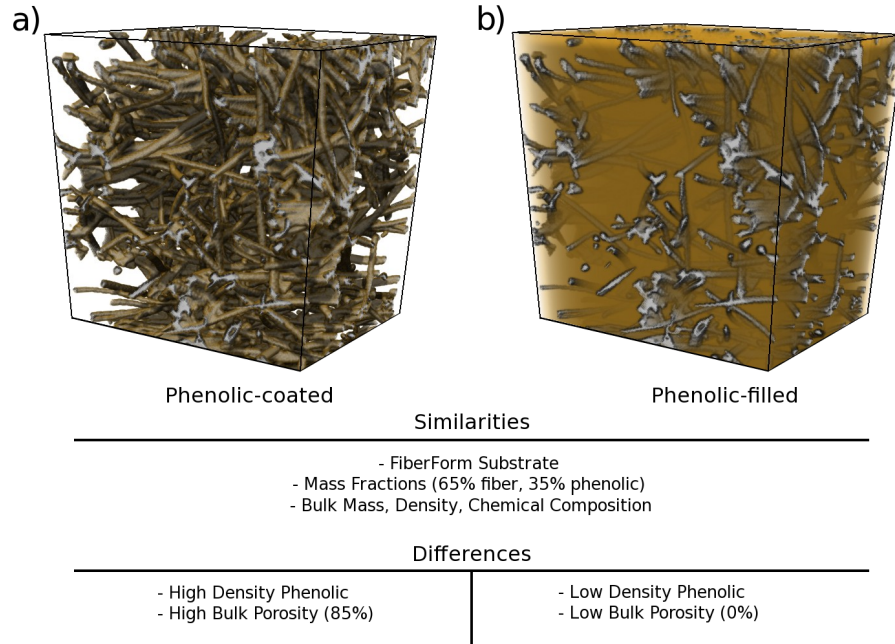


Figure 1: Visualization of two example materials: a) rigid carbon fiber preform coated with high density carbonized phenolic resin, and b) rigid carbon fiber preform filled with low density carbonized phenolic resin.

40 Using the PuMA framework, this study aims at understanding the effects of
 41 the micro-scale structure on the overall oxidation of resin-infused carbon fibers
 42 in order to guide material design. To this goal, we examine the effects of two
 43 carbonized phenolic distributions, shown in Fig. 1, on the micro-scale oxidation
 44 response. These two distributions, representing extreme cases, were selected:
 45 (a) carbon fiber substrate coated with a high density char and (b) carbon fiber
 46 substrate filled with a low density char. The overall mass of the charred ma-
 47 terial is the same in each case. The resulting materials, built upon the same
 48 carbon fiber substrate, have different porosity, but have the same constituent
 49 mass fractions, density, and chemical composition. These distributions are not

50 intended to represent those of existing materials, but rather to serve as a the-
51 oretical model, capturing the extreme cases, to study the micro-scale oxidation
52 and guide future material development.

53 Simulations are performed on ideal geometries as well as on micro-tomography
54 representation of a carbon fiber preform material at various diffusion/reaction
55 regimes for both the phenolic-coated (Fig. 1a) and phenolic-filled (Fig. 1b) cases.

56 Section 2 provides an overview of the simulation tools used in this study.
57 We describe the oxidation model and the numerical method used to solve the
58 diffusion/reaction problem. We also provide details on the use of 3D micro-
59 tomography within the PuMA framework. Section 3 details analytical and
60 numerical studies on ideal geometries, as well as numerical simulations on to-
61 mographic representations of a carbon fiber material available commercially (in
62 this case FiberForm[®]). Section 4 contains the conclusion and outlook.

63 2. Methods

64 2.1. Physical model

For carbon/resin composites, the oxidation reaction of the carbonaceous char
is a main source of material recession during ablation at temperatures below the
sublimation regime. In an oxygen-rich entry plasma, oxidation primarily occurs
via the reaction pathway $C(s) + O \longrightarrow CO$ and, to a lesser extent, via $C(s) +$
 $O_2 \longrightarrow CO_2$ [15? , 16]. Other decomposition mechanisms may also occur under
certain conditions, e.g. sublimation, nitridation, decomposition via reactions
with CO_2 and material removal by shear stresses. For a fibrous char, the local
motion of the carbon/gas interface can be modeled using a differentiable surface
function $S(x, y, z, t)$ [7, 8], as:

$$\frac{\partial S}{\partial t} + \vec{v} \cdot \nabla S = 0, \quad (1)$$

where the recession velocity, \vec{v} , of the surface is

$$\vec{v} = \Omega J \vec{n} \quad (2)$$

Here, Ω is the solid molar volume and \vec{n} is the unit normal vector from the surface. J is the molar oxidation flux. Assuming Fickian mass diffusion and first order oxidation reactions, J is given by

$$J = -D\nabla C \cdot \vec{n} = k_f C \quad (3)$$

65 where D is the diffusion coefficient of the reactant in the bulk fluid phase, k_f
 66 is the intrinsic reactivity [17] of the carbon fiber¹, and $C = C(x, y, z, t)$ is the
 67 local concentration of oxygen.

The conservation of oxygen in the gas phase assuming negligible convection is given by

$$\frac{\partial C}{\partial t} - \nabla \cdot (D\nabla C) = 0 \quad (4)$$

68 An analogous expression to Eq. 3 can be written for the carbonized matrix, with
 69 the intrinsic reactivity of the matrix k_m used in place of k_f [7, 8]. The absolute
 70 values of k_f and k_m are very difficult to characterize, both experimentally and
 71 numerically, and a large scatter of data is found in the literature [17]. However, a
 72 ratio of 1:10 between the intrinsic reactivity of the carbon fibers (usually rayon-
 73 or PAN-based) and that of the matrix is a typical approximation [17], owing to
 74 the larger presence of atomic level defects in amorphous carbon.

75 Analytical solutions of Eqs. 1-4 in ideal porous media have shown that the
 76 oxidation process is controlled by two competing scales, namely the rate of
 77 diffusion of the reactants into the material and their rate of reaction at the
 78 surface[8]. This competition is quantified by the Thiele number, Φ , which for a
 79 single-phase fibrous medium can be defined as

$$\Phi = \frac{d_p}{\sqrt{D_{\text{eff}}/(s_f k_f)}} \quad (5)$$

80 Here, d_p is the mean pore diameter of the medium, D_{eff} is the effective diffusion
 81 coefficient, s_f is the specific surface area, and k_f is the reactivity of the fibers.

¹The intrinsic reactivity of the carbon fiber is not to be confused with the effective reactivity, k_{eff} , which describes, instead, the reactivity of the bulk porous material

82 In the diffusion-limited regime, $\Phi \gg 1$, the high reaction to diffusion ratio
83 yields oxidation that occurs at the first gas surface interface. Conversely, in the
84 reaction limited regime, $\Phi \ll 1$, reactants are able to diffuse in depth into the
85 material prior to oxidizing the surface. In the mixed regime, $\Phi \approx 1$, reactants
86 are able to partially diffuse into the material prior to reacting.

87 The presented model uses a single mesoscopic reactivity value based on em-
88 pirical relations[15]. A higher fidelity study of the material recession should
89 consider the full set of heterogeneous reactions approximated in this reactivity
90 model, including the transport of reaction products[18].

91 *2.2. Numerical method*

92 In order to solve the reaction/diffusion problem described by Eqs. 1-4 on
93 complex porous media, a particle based simulation technique was proposed in
94 [7], and later improved to be run in parallel on large tomography datasets [14].
95 Micro-tomography representations of the material (see section 2.4) are used as
96 a computational domain and are stored as a 3D matrix of grayscale values that
97 correspond to the local material density. Oxygen atoms are represented by
98 particles, called walkers, whose diffusion towards and into the porous material
99 is simulated through a Brownian motion technique [7]. Walkers are initially
100 located in a buffer zone placed at the top of the computational domain, as shown
101 in Fig. 2. A constant concentration of oxygen is maintained in the buffer zone
102 during a simulation, satisfying a Dirichlet boundary condition. As the material
103 recedes, the buffer zone is shifted in the direction of material recession so that
104 the diffusion length to the surface remains constant throughout the simulation.
105 Periodic boundary conditions are used at the side of the domain and a reflective
106 (i.e. insulating) boundary condition on the bottom of the domain.

107 Surface collisions are determined based on a grayscale interpolation method
108 [14] rather than in previous implementations [7] in which collisions were based
109 on a triangle isosurface from a marching cubes algorithm [19]. Surface reces-
110 sion is simulated through a sticking probability law [7, 20]. In the case of a
111 sticking event, the nearest material vertex in the global matrix is reduced by

112 the grayscale attenuation rate [14]. In the case of a non-sticking collision, the
 113 walker is diffusely reflected at a random angle to complete its walk.

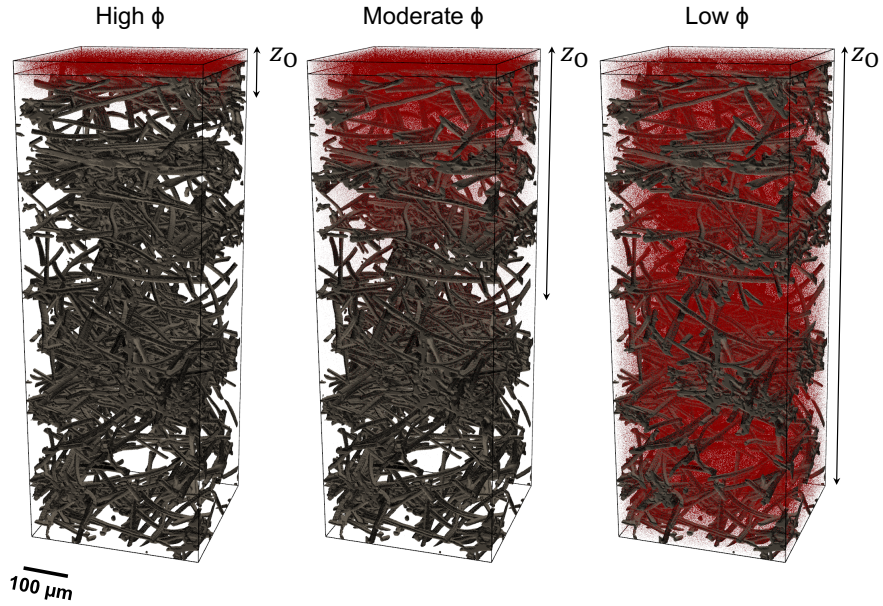


Figure 2: Example simulation domains in three Thiele regimes, showing the carbon fiber preform in gray, walkers in red, and the steady state oxygen diffusion depth, z_0 . The buffer zone, populated with walkers at the top of the domain, is also displayed.

114 *2.3. The PuMA simulation framework*

115 The Porous Materials Analysis (PuMA) was developed to serve as a com-
 116 putational framework for calculating material properties and material response
 117 from micro-tomography data of porous materials [14]. The oxidation model and
 118 numerical method described in section 2.1 and section 2.2, respectively, were im-
 119 plemented into PuMA and were verified against analytical solutions [21].

120 The oxidation model was parallelized using OpenMP [22, 23] for multi-
 121 threaded simulations on a shared memory system. In the parallelization scheme,
 122 walkers are divided into walker groups, with each walker group assigned to a
 123 processor. The random walks are parallelized over the walker groups, with each

124 group running independently over a predefined number of time steps, called a
125 megastep. Each group maintains its initial oxygen concentration in the buffer
126 zone for every time step; the aggregate of these conditions maintains the in-
127 tegrity of the Dirichlet boundary condition.

128 The speed increase scales approximately linearly with the number of proces-
129 sors available on a shared-memory system. Utilizing all 36 processors on the
130 test machine, a 25 fold speed increase was observed. The parallelization of the
131 oxidation model allows for the simulation of oxidation in the low Thiele regime
132 on large datasets, which would otherwise have had prohibitively long run times.

133 *2.4. Computational domains from X-ray micro-tomography*

134 Micro-tomography has become a very useful tool for material science ap-
135 plications [12] [13], allowing for non-destructive characterization of a material
136 microstructure at a sub-micron scale. For this study, X-ray micro-tomography
137 imaging of FiberForm was performed at the Advanced Light Source (ALS) at
138 Lawrence Berkeley National Laboratory [11]. FiberForm is the fibrous sub-
139 strate of the Phenolic Impregnated Carbon Ablator (PICA), a state-of-the-art
140 lightweight ablator with a record of successful use in several NASA missions.
141 Details about micro-tomography imaging and reconstruction of FiberForm are
142 provided in previous publications [10, 14]. A visualization example, obtained
143 using a threshold-based marching cubes segmentation procedure implemented
144 in PuMA is shown in Fig. 2. For the results presented in section 3, we used
145 tomography volumes of $0.5 \text{ mm} \times 0.5 \text{ mm} \times 1 \text{ mm}$, with a voxel size of $1.3 \text{ }\mu\text{m}$.
146 This voxel size provides an accurate resolution of the material microstructure
147 [24].

As the purpose of this study is to examine the effects of charred resin dis-
tribution (the two extremes of which are shown in Fig. 1), attempts were made
to use microtomography of impregnated samples of FiberForm, but were not
successful due to the low density (and X-ray absorption) of the carbonized ma-
trix. However, algorithms were developed to numerically add the matrix to the
carbon fiber substrate. For the phenolic-coated case, fibers were coated with a

matrix of approximately $r_m = \sqrt{2}r_f$, doubling the solid volume fraction of the domain. To create the matrix, intersecting spheres of the desired radius were created around each material edge voxel within the domain; the combination of these spheres resulted in a good approximation of a uniform coating. For the phenolic-filled case, the matrix was evenly distributed throughout the domain. Both the filling matrix and the coating matrix were given a mass fraction $x_m = 0.35$. Therefore, the density and chemical compositions of the bulk material remained unchanged for the two cases. The intrinsic density of the matrix phase in each case is found through the following mass balance:

$$\frac{\rho_m \epsilon_m}{x_m} = \frac{\epsilon_f \rho_f}{x_f} \quad (6)$$

148 where ρ is the density, ϵ is the volume fraction, and x is the mass fraction. The
 149 subscripts f and m denote fiber and matrix, respectively.

150 **3. Results and discussion**

151 *3.1. Modeling of ideal geometries*

152 In a previous work, an analytical solution of the steady state oxidation was
 153 derived for a fiber parallel to a reactant concentration gradient, surrounded by
 154 a matrix of higher reactivity [21]. This analytical model provides the shape
 155 and height of the oxidized fiber at combinations of matrix-to-fiber reactivity
 156 contrast A (defined later) and Sherwood number. The analytical solution was
 157 used in [14] as a verification of the oxidation model implemented in PuMA. As
 158 the present study focuses on transverse isotropic fibrous media, we extended the
 159 analytical solution to an array of infinite, parallel cylinders perpendicular to the
 160 reactant concentration gradient, which more closely resembles the properties of
 161 the actual material. Figure 3 shows a single fiber isolated from the two ideal
 162 geometries analyzed: cylindrical fibers coated by a high density matrix layer
 163 and cylindrical fibers immersed in a uniform low density matrix that occupies
 164 the entire void space. The two cases are referred to as “matrix-coated” and
 165 “matrix-filled”, respectively.

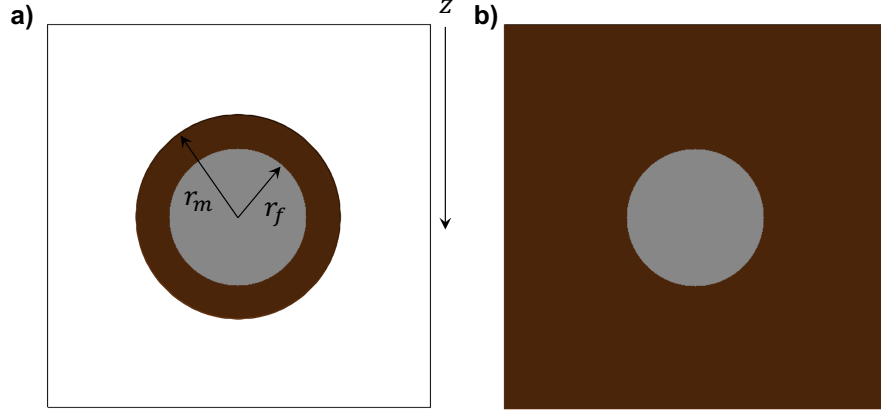


Figure 3: Schematic of single fiber isolated from ideal geometries considered in this study: a) fibers coated with high density matrix, and b) fibers filled with a uniform low density matrix. Fiber and matrix are displayed in gray and brown colors respectively.

For the two geometries of Fig. 3, one can write [8]:

$$\frac{d\vec{r}_f}{dt} = -\Omega_f k_f C_z \vec{e}_r \quad (7)$$

for the recession velocity of the fiber, and

$$\frac{d\vec{r}_m}{dt} = -\Omega_m k_m C_z \vec{e}_r \quad (8a)$$

$$\frac{d\vec{z}}{dt} = \Omega_m k_m C_z \vec{e}_z \quad (8b)$$

166 for the recession velocity of the matrix for the cases of Fig. 3a and Fig. 3b. \vec{e} is
 167 the unit vector of the orientation of the surface. C_z is the concentration of the
 168 reactant at depth z and is assumed to be uniform in the x - y plane. Although
 169 Eqs. 7-8b are valid at every Thiele regime, the exact value of C_z is only known for
 170 a reaction-limited case, where the concentration at every point can be assumed
 171 to be equal to the concentration in the buffer zone, C_0 .

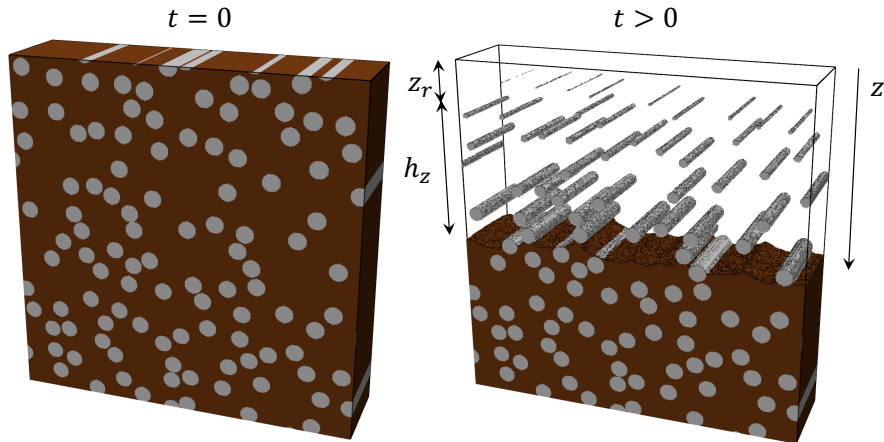


Figure 4: Schematic of randomly positioned cylinders perpendicular to the reactant concentration gradient prior to (left) and during (right) oxidation.

For the matrix-filled case in the low Thiele regime, an approximate analytical solution for the steady-state reaction depth can be found from Eq. 7 and Eq. 8b. As shown in Fig. 4, we define z and z_r as the depth of matrix and fibers recession front, respectively. For an infinite random array of cylinders, z_r becomes the depth of the midpoint of the highest cylinder that has not fully receded. The overall recession depth becomes $h_z = z - z_r$. The depth of the matrix at time t is found by integrating Eq. 8b from 0 to t and assuming that the matrix recedes uniformly in z :

$$z(t) = \Omega_m k_m C_0 t \quad (9)$$

172 For the fibers, it is assumed that each cylinder recedes uniformly in the radial
 173 direction and only begins receding when the matrix has passed the midpoint of
 174 the given cylinder. This assumption holds approximately true for $A > 2$, where
 175 A is the matrix-to-fiber reactivity contrast, $A = \Omega_m k_m / \Omega_f k_f$.

We define t_r to be the time for the matrix to reach the midpoint of the

highest fiber that has not fully receded. From Eq. 9, t_r is found to be

$$t_r = \frac{z_r}{\Omega_m k_m C_0} \quad (10)$$

The radius of the highest cylinder that has not fully receded is found by integrating Eq. 7 from t_r to t . Hence, we have:

$$r_f(t) = r_{f,0} \quad \text{for } t \leq t_r \quad (11a)$$

$$r_f(t) = r_{f,0} - \Omega_f k_f C_0 (t - t_r) \text{ for } t > t_r \quad (11b)$$

From Eq. 11b, the matrix depth below the highest cylinder can then be obtained by computing t and t_r from Eq. 9:

$$r_f(t) - r_{f,0} = -\frac{\Omega_f k_f}{\Omega_m k_m} (z - z_r) \quad (12)$$

or

$$h_z(t) = A(r_{f,0} - r_f(t)) \quad (13)$$

At steady-state, where $\frac{dz}{dt} = \frac{dz_r}{dt}$ and the radius of the highest cylinder approaches 0, Eq. 13 becomes

$$h_z^\perp = A r_{f,0} \quad (14)$$

This solution is valid for $A \gg 1$. For fibers parallel to the reactant concentration gradient, fully surrounded by a reactive matrix, it has been shown in [21] that the steady state height of the fiber is calculated as:

$$h_z^\parallel = r_{f,0} \sqrt{A^2 - 1} \quad (15)$$

Interpolating between Eq. 14 and Eq. 15, an approximate solution for the reaction depth of randomly oriented cylinders is found to be:

$$h_z = \left(\frac{2\theta}{\pi}\right) r_{f,0} \sqrt{A^2 - 1} + \left(1 - \frac{2\theta}{\pi}\right) r_{f,0} A \quad (16)$$

176 where θ is the average magnitude of the angle between the cylinders and the
177 perpendicular plane, $\theta \in [0, \pi/2]$. For $A \gg 1$, the solution converges to Eq. 14.

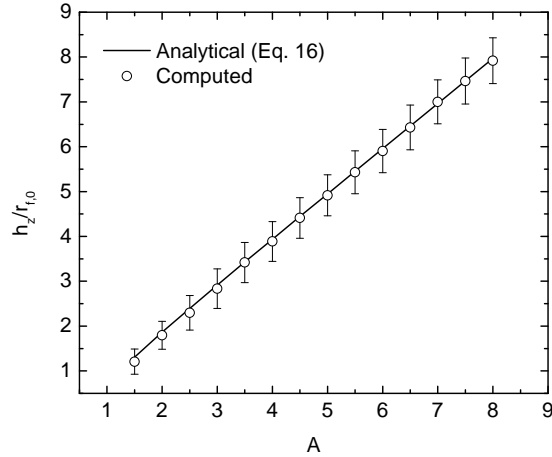


Figure 5: Comparison between the analytical solution in Eq. 16 and PuMA simulations in the low Thiele regime at increasing reactivity contrasts A , performed using a digital carbon/phenolic composite with randomly-oriented cylindrical fibers.

178 Figure 5 shows the steady state reaction depth for randomly oriented cylin-
 179 ders ($\theta = \pi/4$) in the low Thiele regime as a function of the reactivity contrast.
 180 The tested geometries had a porosity $\epsilon = 0.85$. Since the matrix recession is not
 181 uniform (as seen in Fig. 4), the reaction depth was calculated by subtracting
 182 the average highest voxel containing matrix in the points on the x - y plane from
 183 the highest point in the domain containing a fiber voxel. Error bars indicate
 184 the variation in matrix depth within the x - y plane. The values were averaged
 185 over approximately 100 time increments to reduce numerical fluctuations. The
 186 randomly oriented cylinders exhibit, on the average, the behavior predicted by
 187 Eq. 16.

188 For the matrix-coated case, shown in Fig. 3a in the low Thiele regime, there
 189 is no steady state oxidation depth as the entire surface recedes uniformly due to
 190 the constant concentration, C_0 . However, a transient solution is possible from
 191 Eq. 7 and Eq. 8a. Integrating Eq. 8a from 0 to t , the radius of the matrix for

192 $r_m(t) > r_{f,0}$ is found to be

$$r_m(t) = r_{m,0} - \Omega_m k_m C_0 t \quad (17)$$

When $r_m(t) = r_{f,0}$ at time t_m , the matrix is fully oxidized and the fiber recession begins. Integrating Eq. 7 from t_m to t , the fiber radius is found to be

$$r_f(t) = r_{f,0} - \Omega_f k_f C_0 (t - t_m) \quad (18)$$

193 for $r_f(t) > 0$ The total recession time for the composite material is found to
194 be

$$t_r = \frac{r_{m,0} - r_{f,0}}{\Omega_m k_m C_0} + \frac{r_{f,0}}{\Omega_f k_f C_0} \quad (19)$$

195 Simulations in the low Thiele regime were run on a single fiber of radius
196 $r_f = 20\mu\text{m}$ coated with a matrix of $r_m = 10\mu\text{m}$, varying the reactivity contrast
197 between $A = 1$ and $A = 10$. The radius evolution in time was compared to the
198 analytical solutions presented in Eq. 17 and Eq. 18 and shown in Fig. 6. The
199 solutions produce good agreement until the radius decreases until the cylindrical
200 shape is no longer accurately captured in the Cartesian grid, around $r_f = 4$
201 voxels.

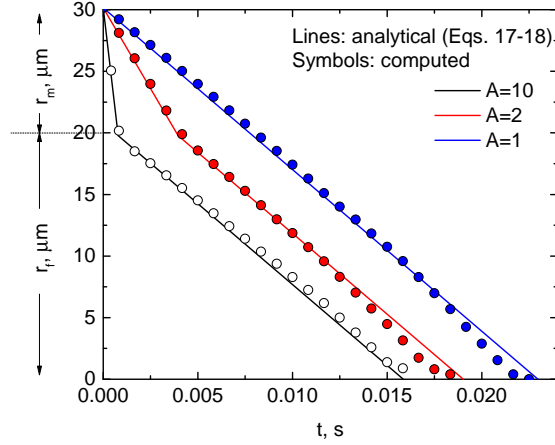


Figure 6: Comparison between the analytical solution in Eq. 17 and Eq. 18 and PuMA simulations at reactivity contrasts of 1, 2, and 10 on a single fiber of $r_f = 20\mu\text{m}$ coated with a matrix of $r_m = 10\mu\text{m}$.

202 3.2. Simulations on carbon fiber substrates

203 Simulations were then performed on micro-tomography domains of a real
 204 carbon fiber preform in order to observe the effect of resin matrix distribution
 205 on a complex geometry. A carbonized phenolic matrix is added to a $520\mu\text{m} \times$
 206 $520\mu\text{m} \times 1040\mu\text{m}$ micro-tomography sample of FiberForm with a reactivity
 207 of $5k_f$. For the phenolic-coated case, shown in Fig. 1a, the matrix is applied as
 208 a coating over the carbon fiber substrate with a radius of $\approx 2.5\mu\text{m}$, such that
 209 the solid volume is doubled.

210 In the phenolic-filled cases, shown in Fig. 1b, the matrix is evenly distributed
 211 in all of the material voids. For an assumed carbon fiber density of ≈ 1700
 212 kg/m^3 , and an imposed 35% mass fraction of the matrix for both cases, the
 213 phenolic-coated case matrix is found to have a density of $\approx 850\text{ kg}/\text{m}^3$. For
 214 the phenolic-filled case, the carbonized phenolic matrix density is $\approx 150\text{ kg}/\text{m}^3$.
 215 These values vary slightly depending on the sample used, given the small scale of
 216 the micro-tomography, the inhomogenous nature of the carbon fiber substrate,
 217 and the high uncertainties in manufacturer specifications.

218 Oxidation was then simulated in each of the three regimes on both the

219 matrix-filled and matrix-coated cases in order to examine the differences in
220 micro-scale oxidation characteristics based on the carbonized phenolic matrix
221 distribution. In both cases, the Thiele number of the simulation was varied
222 between 0.005 and 50, covering the full range of regimes. Figures 7, 8, and 9
223 show the evolution in time of the oxidation reaction at various Thiele numbers.

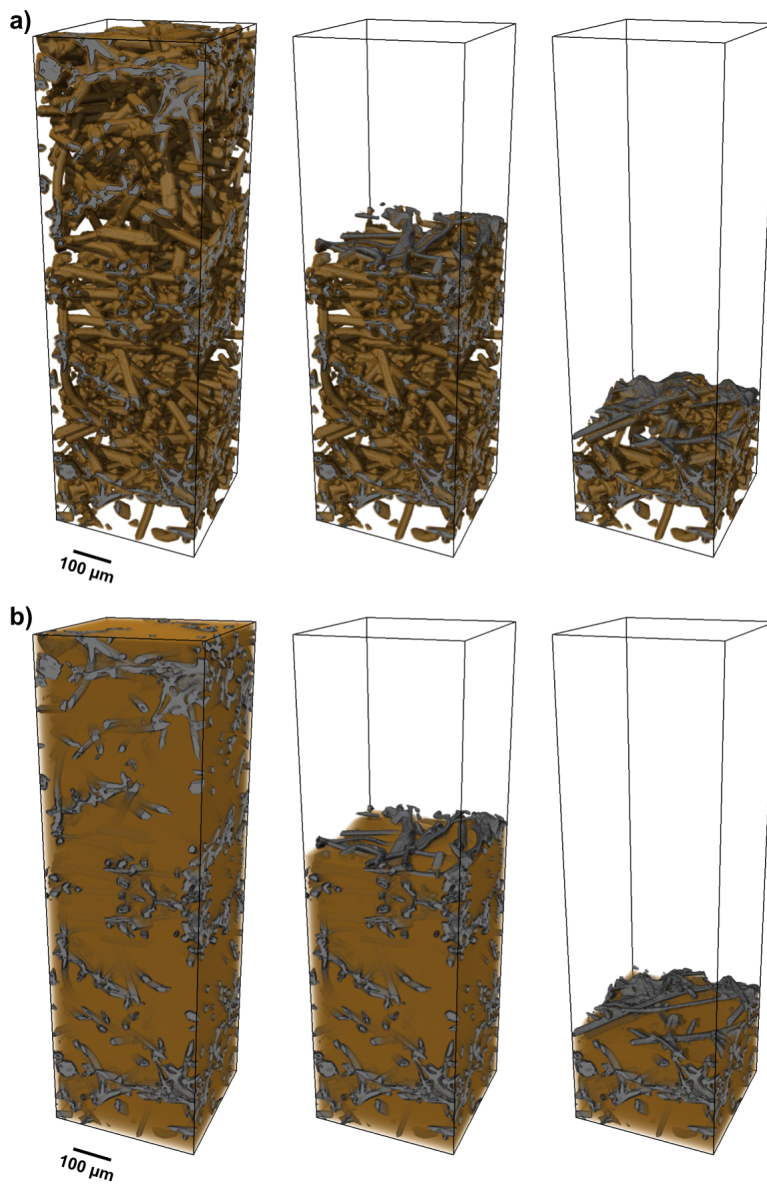


Figure 7: Visualizations of in-depth oxidation in the high Thiele regime ($\Phi = 50$) for a) FiberForm coated in a high density carbonized phenolic matrix (phenolic-coated case) and b) FiberForm filled with a low density carbonized phenolic matrix (phenolic-filled case).

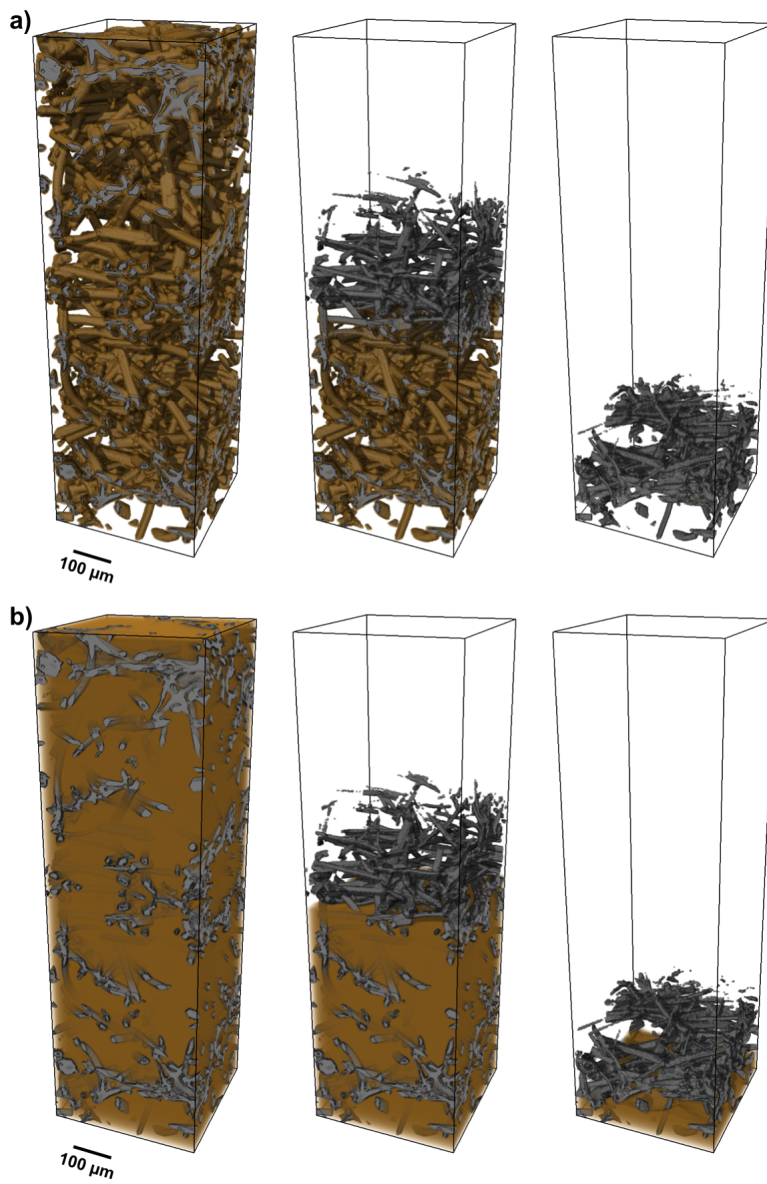


Figure 8: Visualizations of in-depth oxidation in the moderate Thiele regime ($\Phi = 0.5$) for a) FiberForm coated in a high density carbonized phenolic matrix (phenolic-coated case) and b) FiberForm filled with a low density carbonized phenolic matrix (phenolic-filled case).

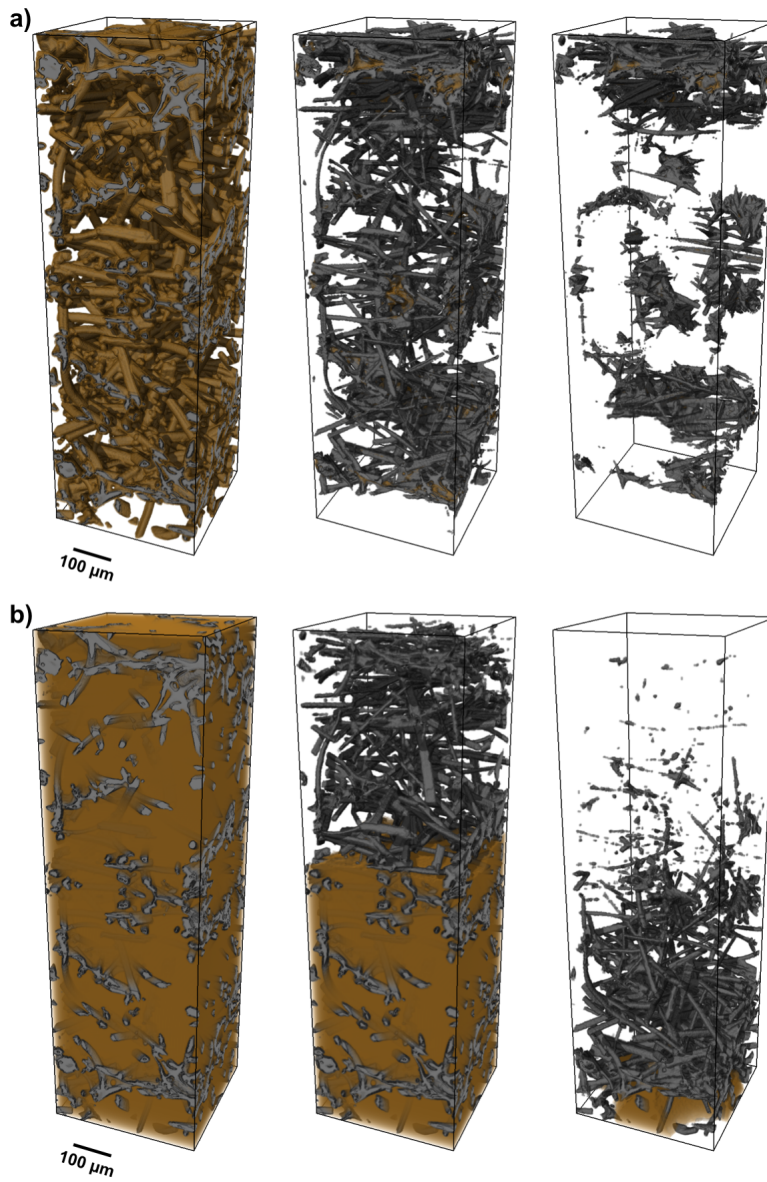


Figure 9: Visualizations of in-depth oxidation in the low Thiele regime ($\Phi = 0.005$) for a) FiberForm coated in a high density carbonized phenolic matrix (phenolic-coated case) and b) FiberForm filled with a low density carbonized phenolic matrix (phenolic-filled case).

225 function of the Thiele number. At $\Phi = 50$, both the phenolic-coated and the
226 phenolic-filled cases are fully oxidizing in the surface ablation regime. For a
227 moderate Thiele number, $\Phi = 0.5$, the reactants are able to partially diffuse
228 into the material prior to the oxidation reaction, operating in the mixed regime.
229 For very low Thiele numbers, $\Phi = 0.005$, the reactants fully diffuse into the
230 material and oxidize all exposed surfaces simultaneously, in the volume ablation
231 regime. The in-depth evolution over time of the materials is shown in Fig. 10,
232 which gives the in-depth bulk density change at multiple time steps for the cases
233 presented in Figs. 7-9.

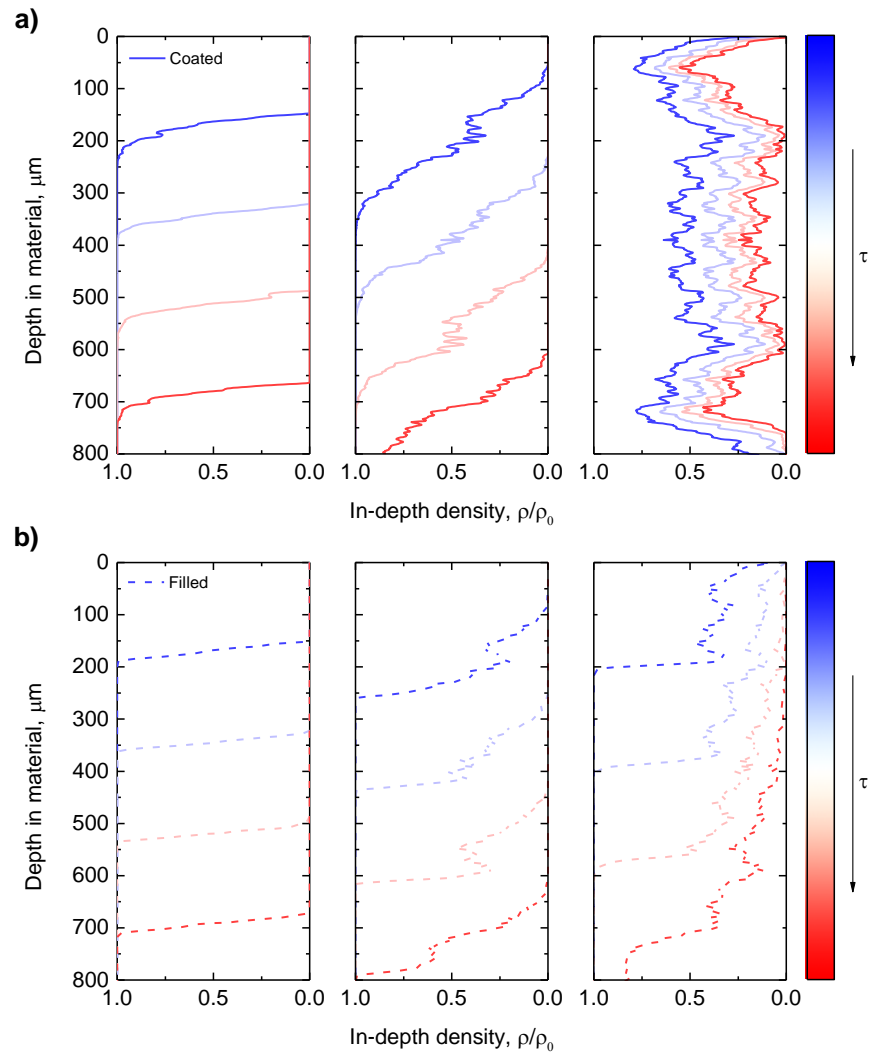


Figure 10: In-depth bulk density change at multiple time steps for a) FiberForm coated in a high density carbonized phenolic matrix (phenolic-coated) and b) FiberForm filled with a low density carbonized phenolic matrix (phenolic-filled). Panels from left to right show decreasing Thiele numbers: $\Phi = 50$, $\Phi = 0.5$, and $\Phi = 0.005$.

235 depth can be measured as the difference in depth between the fully oxidized
236 material ($\rho_z/\rho_0 = 0$) and the virgin material ($\rho_z/\rho_0 = 1$). For all but the
237 $\Phi = 0.005$ phenolic-coated case, the time progression is from the top of the figure
238 to the bottom. For the $\Phi = 0.005$ phenolic-coated case, since the oxidation is
239 in the volume ablation regime, the time progression is from the left to the right
240 of the figure.

241 It can be seen in Fig. 10 that in high Thiele cases, the simulation quickly
242 reaches steady state, where the recession velocity of the fibers and the phenolic
243 converge, for both matrix distributions. The overall oxidation depth is shallow
244 enough that there is no clear distinction between the oxidation zones of the two
245 phases (carbon fibers and carbonized phenolic) in either the phenolic-coated
246 or phenolic-filled cases. There is little difference in the micro-scale oxidation
247 behavior of the two cases in high Thiele cases.

248 For a moderate Thiele number, shown in Fig. 10 as $\Phi = 0.5$, a steady state
249 is also reached for both cases. However, the two phases produce two distinct
250 oxidation zones, with noticeable differences beginning to emerge in the oxidation
251 behavior between the phenolic-coated and phenolic-filled cases.

252 For low Thiele numbers, shown in Fig. 10 as $\Phi = 0.005$, there exist large
253 differences in the oxidation behavior between the two cases, as predicted by the
254 study on ideal fibers in section 3.1. For the phenolic-coated case, the mate-
255 rial recedes uniformly in-depth and no steady state is reached. Once the entire
256 coating is oxidized, the recession rate slows significantly due to the decreased
257 reactivity and available surface area. For the phenolic-filled case, matrix re-
258 cedes and the exposed carbon fibers are uniformly oxidized. For this case, the
259 simulation eventually reaches a steady state.

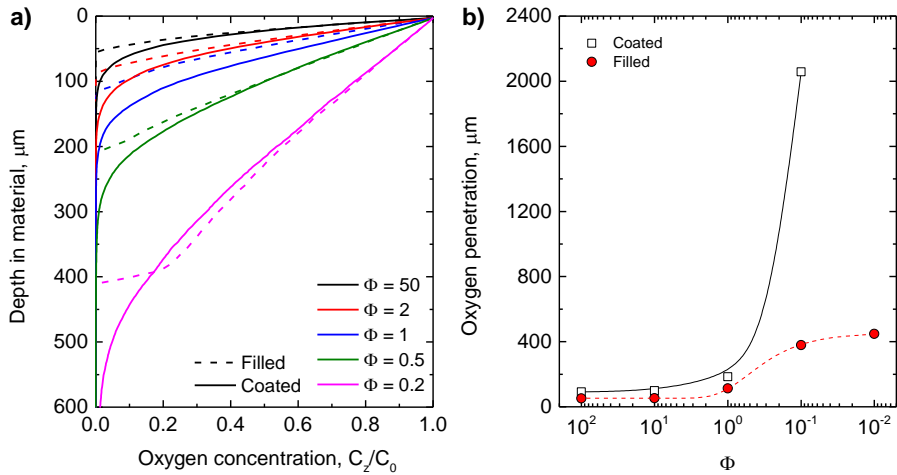


Figure 11: (a) Steady state oxygen concentration in depth at various Thiele numbers for both the matrix-filled and matrix-coated cases. (b) Oxygen penetration depth as a function of Thiele number for the matrix-filled and matrix-coated cases.

260 Figure 11a shows the in depth oxygen concentration at various Thiele num-
 261 bers for the two cases, showing that for $\Phi > 2$ the differences in oxygen pen-
 262 etration between the two cases remain relatively small. Figure 11b shows the
 263 steady state oxygen penetration depth, with a cutoff at 2% of the reservoir con-
 264 centration. The domains used in Figs. 7-9 were mirrored in the z direction to
 265 reach the necessary depth for the low Thiele cases. We find that the carbonized
 266 phenolic distribution results in significant changes in the oxygen penetration in
 267 the low Thiele regime. In this regime, a steady state oxidation depth is reached
 268 in the matrix-filled case, while the solution diverges in the matrix-filled case as
 269 the Thiele number approaches 0. The in-depth oxygen concentration, as well as
 270 the available surface area and reactivity of each phase can be used to determine
 271 the theoretical steady state oxidation rate of the materials.

272 The results shown in Figs. 10-11 demonstrate that at high reactivities, there
 273 is little difference in the oxidation behavior of carbon phenolic ablators based
 274 on the distribution of carbonized phenolic matrix. As the reactivity and Thiele
 275 number decrease, large differences develop in the oxidation behavior that are

276 not captured in heritage surface ablation models. Moreover, these differences
277 lead to significant changes in the effective reactive surface area, which is critical
278 for determining oxidation reaction rates. It is important to note that this study
279 only examined the oxidation reaction and did not account for the mass loss
280 due to sublimation or spallation. However, this method has the potential to
281 provide insight into the effect of Thiele number and matrix distribution on the
282 evolution of average fiber radius in the oxidation zone, which may prove useful
283 in the modeling of spallation or other mechanical phenomena.

284 **4. Conclusion**

285 A micro-scale oxidation model was used to study the recession of carbon
286 fibers impregnated with a highly reactive phenolic matrix. Analytical and nu-
287 merical modeling were carried out on ideal fiber clusters, demonstrating that
288 the oxidation behavior can be predicted on randomly oriented cylinders in the
289 low Thiele regime. Simulations were then conducted on a micro-tomography
290 sample of a carbon fiber preform. It was shown that the oxidation depth is a
291 strong function of the Thiele number, with little effect produced by the matrix
292 distribution at high Thiele number. However, at low Thiele numbers, the car-
293 bonized phenolic matrix distribution plays a significant role in the micro-scale
294 oxidation characteristics. These effects must be considered in volume averaged
295 (phenomenological) models, particularly the role of the matrix distribution on
296 the effective reactive surface area and the oxidation depth.

297 Future work will include the introduction of heat transfer and thermal gra-
298 dients in order to develop a more physically realistic model. Additionally, a
299 more complex gas model will be included to improve the fidelity of the diffusion
300 and surface reactions, as well as the transport of oxidation products (CO and
301 CO₂) out of the material. Pyrolysis gas transport will also be considered in
302 future works. The production and blowing of pyrolysis gases is likely to affect
303 the diffusion of reactants into the porous media. In addition, pyrolysis gases
304 may react with species from the freestream flow, with oxidation products, as

305 well as with the material itself. The work presented in this paper, as well as
306 future work, will be used to feed next generation volume averaged models, with
307 the ultimate goal of informing future material design.

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